Atomic and nuclear physics
X-ray physics
X-ray tomography

Objects of the experiment
- Understanding the material absorption of the X-rays.
- Understanding the 3D-image reconstruction used for the computed tomography.
- Device adjustment and graphical tools for biological tissue identification.

Principles

The initial intensity \( I_0 \) of an X-ray beam is reduced after passing through a homogeneous material according to the Lambert law

\[
I_s = I_0 e^{\mu s},
\]

(1)

Here is \( I_s \) the resulting beam intensity, \( s \) the length of the way through the material and \( \mu \) the material absorption coefficient. The latter has the physical dimension 1/Length and is material specific, depending a.o. on the material density, atomic number and the energy (wavelength) of the beam. Absorption coefficient reveals therefore material distribution, knowledge of which is of a great importance in medicine and other fields.

For inhomogeneous materials the constant absorption coefficient \( \mu \) is replaced by \( \mu(s) \) and the exponent in eq. (1) becomes an integral

\[
\ln \frac{I_s}{I_0} = - \int s \mu(s') ds'.
\]

(2)

For a general absorption coefficient \( \mu = \mu(x',y,z) \), given as a function on the three dimensional space, the integral in eq. (2) is written as a path integral

\[
\ln \frac{I_s}{I_0} = - \int s \mu(x(s'),y(s'),z(s')) ds'
\]

(3)

along the straight beam path. For a fixed plane \( \Sigma \) (in the three dimensional space) parametrized by a coordinate system \( (x',y) \), any line is given by the slope \( m \) and the \( y \)-intersect \( b \). For a function \( \mu(x',y') \) on the plane \( \Sigma \) the integral along the line given by \( (m,b) \) is a functional assignment

\[
(m,b) \mapsto \int_{x'}^{x''} \mu(x', mx'+b) dx',
\]

(4)

called the Radon transformation. According to the Radon’s theorem (J. Radon (1917)), the function \( \mu(x',y') \) can be reconstructed if function’s integral is known for all \( (m,b) \).

Computed tomography (CT) is a direct application of Radon’s theorem. According to eq. (3) a line integral of the absorption coefficient \( \mu \) along the beam path in a sectional plane of a body is given by the logarithm of intensity fraction. Measuring therefore intensity fraction for many lines, absorption coefficient \( \mu \) can be reconstructed. Its graphical representation reveals the sectional plane compound structure. Substance identification with application to medicine is studied in experiments P6.3.8.3-4 and P6.3.8.13-14. A CT measurement scheme is shown in fig. 1. Intensity fraction measurement for many lines is realized by the rotation of the body.

Measurement with the computed tomography module

Measurement time restricts the number of rotation angles. A high-pass filter is therefore applied to measured data before reconstructing \( \mu \). A high-pass filter highlights boundaries of different materials (like bones and organs in a human body) as it amplifies the contrasts. It reduces therefore errors caused by the finite number of measurements. This procedure is called the filtered Radon back transformation and is the key of the CT algorithm.

The number of rotations and the used high-pass filter influence image quality and its resolution. The resolution is also restricted by the pixel size of the detecting device. A further source of image quality error is the continuous X-ray spectrum. Eq. (1) holds only for the monochromatic beam. Passing through material, the X-ray beam spectrum is shifted to higher energies. This effect is called beam hardening and is studied in experiments P6.3.8.4 and P6.3.8.14. Absorption coefficient values in the whole body are obtained by combining measured data for different sectional planes. In this case the smallest image unit is called a voxel. Graphical representation of \( \mu \) is the end result of the computed tomography.

The 1979s Nobel Prize in Physiology or Medicine was awarded to Allan M. Cormack and Godfrey N. Hounsfield for their development and application of computed tomography.
In this experiment a CT scan of a frog is done. Using CT software’s graphical tools, spatial tissue distribution in the frog, like bones, muscles and even skin, can be visualized. This is a CT’s big advantage compared to a single X-ray image, from which only hard materials, like bones und metals, are seen. Furthermore, students learn device adjustment, sources of errors and resolution restrictions.

Setup

- Insert the Au tube in the X-ray apparatus.
- Mount the goniometer in the X-ray experiment chamber and move it to the right side. Fix the goniometer using the two screws in its lower part.
- Put the computed tomography module on the right side of the X-ray apparatus and connect the latter to the computed tomography module using a USB cable.
- Connect the computed tomography module to a PC using a USB cable.

Camera adjustment

**Note**

Camera adjustment must be performed prior to the measurement.

- Turn on the PC, the X-ray apparatus and the computed tomography module.
- Start the CT software and find the expandable tabs on the left.
- Choose the video device (fig. 2: 3 und 4) and turn it on (fig. 2: 1) while X-ray beam and high-voltage are off (fig. 3: 2).
- Identify defective pixels and correct (fig. 2: 6 and 7).
- Turn on the X-rays (fig. 3: 1).
- Record a white image averaging over app. 10 images and use this as a reference image (fig. 2: 8 und 9).
- Turn off the X-rays (fig. 3: 2).

**Rotary axis adjustment**

**Note**

Rotary axis adjustment must be performed after every new device setup.

- Fasten a rubber band on the tip of the PMMA arms of the object holder to keep the empty holder stable.
- Mount the object holder into the goniometer and close the X-ray apparatus.
- Turn on the X-rays.

In the now visible X-ray image of the object holder, the prolonged rotation axis should appear horizontal in the middle of the image and coincide with the red line. In case of clearly seen misalignment turn off the X-ray radiation and make a rough camera adjustment. Use the screws around the camera inside the CT module to tilt and roll. The two screws on the left hand side of the optical axis must be rotated in the same amount. Close the computed tomography module and turn on the X-rays and the camera. Carry out a measurement keeping all settings as shown in Figs. 2 – 4 by clicking on the button.

After the measurement the X-rays are switched off automatically. Perform the following steps:

- Change to the 2D view by clicking on the button in the upper toolbar.
- Move the slider in the bottom to the left until a sectional plane close to the rubber band is shown on the screen (compare fig. 6).
- Vary the rotary axis value (fig. 5: 1) until the double contours are roughly minimal (fig.6: b).
- Press “1st position” button (fig. 5: 2) and wait until the software optimizes the position.
- Move the slider in the bottom to the right until a sectional plane close to the object holder's bottom plane is shown on the screen.
- Vary the rotary axis value (fig. 5: 1) until the double contours are minimal (fig.6: b).
- Press “2nd position” button (fig. 5: 3) and wait until the software optimizes the position.
- Turn off the X-rays and adjust camera position using the screws in a way the CT software suggest (fig.5: 4, 5 and 6).
Carrying out the experiment

- Carry out the upper steps for the camera and the rotary axis adjustment.
- Increase the number of projections (fig. 4: 1) to 360 or higher depending on the graphic card.
- Unmount the object holder from the goniometer and mount the holder with the frog instead.
- Carry out a measurement keeping all other settings as shown in figs. 2 – 4.

During the measurement, the image reconstruction can be observed in 2D as well as in 3D mode. Use the 2D and 3D buttons in the upper toolbar to change modes. The image is gradually getting better as more and more angular steps are done and taken into account in the Radon transformation.

In 2D mode image representation can be changed between “Projection”, “Log projection” and “Filtered log projection” (fig. 7: 1). In this way we can visualize the difference between the standard X-ray image and the filtered projections used for the CT image reconstruction.

Evaluation

A detailed description of the software is available in the instruction sheet. Please see the manual for catalogue number 554821. Use buttons in CT software’s the upper tool bar to activate different modes and tools.

a) 2D and 3D modes

Use the 2D and the 3D buttons in the upper toolbar to switch the modes. After a mode is chosen, different graphical tools can be activated.

In 2D mode it can be changed between different sectional planes. Use the slider in the bottom. Change displays between “Projection”, “Log projection” and “Filtered log projection” (fig. 7: 1).

b) Arbitrary sectional plane

Use the button in the upper toolbar while in 3D mode to change the representation between the selected sectional plane or the selected sectional plane and the rest of the scanned object behind it. If the button is active, the sectional plane shown on the screen can be chosen for radiographic evaluations by clicking on the button.

c) Switching light on

Use the button to turn on a virtual light source, which amplifies the CT-scan’s 3D impression. Expand the “Light Parameters” (fig. 8) to change settings.

d) Intensity and transparency

In the “Intensity and Transparency” tab (fig. 9) different representation options can be set up. The upper slider (fig. 9: 1) changes the image intensity while the lower slider (fig. 9: 2) changes the transparency. If the transparency is set to a high level, then all soft tissues appear transparent. In this way tissues like bones can be visualised. Additionally, \( \mu \) values can be restricted to a desired range. Use the sliders in the bottom of the “Intensity and Transparency” tab (fig. 9: 3 - 4). In this way only a certain tissue will be shown. This useful for tumours identification or single organs analysis.
e) Stereoscopic view

An even stronger 3D effect is achieved by activating the stereoscopic view with the button. The image in this mode must be viewed through the anaglyph (red-cyan) glasses.

![Intensity and Transparency](image1.png)

Fig. 4: Intensity and transparency: 1: Intensity, 2: Transparency, 3: Lower transparency limit, 4: Upper transparency limit, 5: Reset settings.

Measuring example

![Intensity and Transparency](image2.png)

Fig. 10: Low transparency mode. The visible range is not restricted.

Soft tissues and surfaces are visualized in the low transparency mode (fig. 10). Fig. 11 shows a frog’s CT example for this setting with the full visible range. A virtual light source (right column) highlights surface shaping.

Hard tissues are visualized in the high transparency mode (fig. 12). Fig. 13 shows a frog’s CT example for this setting with the full visible range. A virtual light source (right column) highlights surface shaping.

Soft tissues inside a hard envelope (like bone marrow) can be visualized in the low transparency mode, restricting the visible range to low $\mu$ values (fig. 14).
Fig. 14: Low transparency mode. The visible range is restricted to low $\mu$ values.

Fig. 15: Frog’s CT scan with low transparency level and visible range restricted to low $\mu$ values (fig. 14). Right column includes a virtual light source (is activated using the button).

Fig. 15 shows a frog’s CT example for this setting with the visible range restricted to low $\mu$ values. A virtual light source (right column) highlights surface shaping. In the case of the frog, an empty skin envelope appears on the screen.