

## One-sided and two-sided lever

### Objects of the experiment

- Measuring the force  $F_1$  for a one-sided and two-sided lever as a function of the load  $F_2$ .
- Measuring the force  $F_1$  for a one-sided and two-sided lever as a function of the load arm  $x_2$ .
- Measuring the force  $F_1$  for a one-sided and two-sided lever as a function of the power arm  $x_1$ .

### Principles

A lever is defined as a rigid body rotating on a fixed pivot (often called the fulcrum) which can be used to raise and move loads. The segments from the pivot to the point of application of the force and to the load are termed the lever arms, specifically the power and load arms respectively. In a two-sided lever, the force  $F_1$  and the load  $F_2$  act in the same direction on opposite sides of the pivot; in a one-sided lever, the forces act in opposite directions on the same side of the pivot. The law of levers applies for both lever types:

$$F_1 \cdot x_1 = F_2 \cdot x_2$$

$x_1$ : power arm,  $x_2$ : load arm

This law can be explained on the basis of the more general concept of equilibrium of angular momentums and forms the basis for all types of mechanical transmission of force.

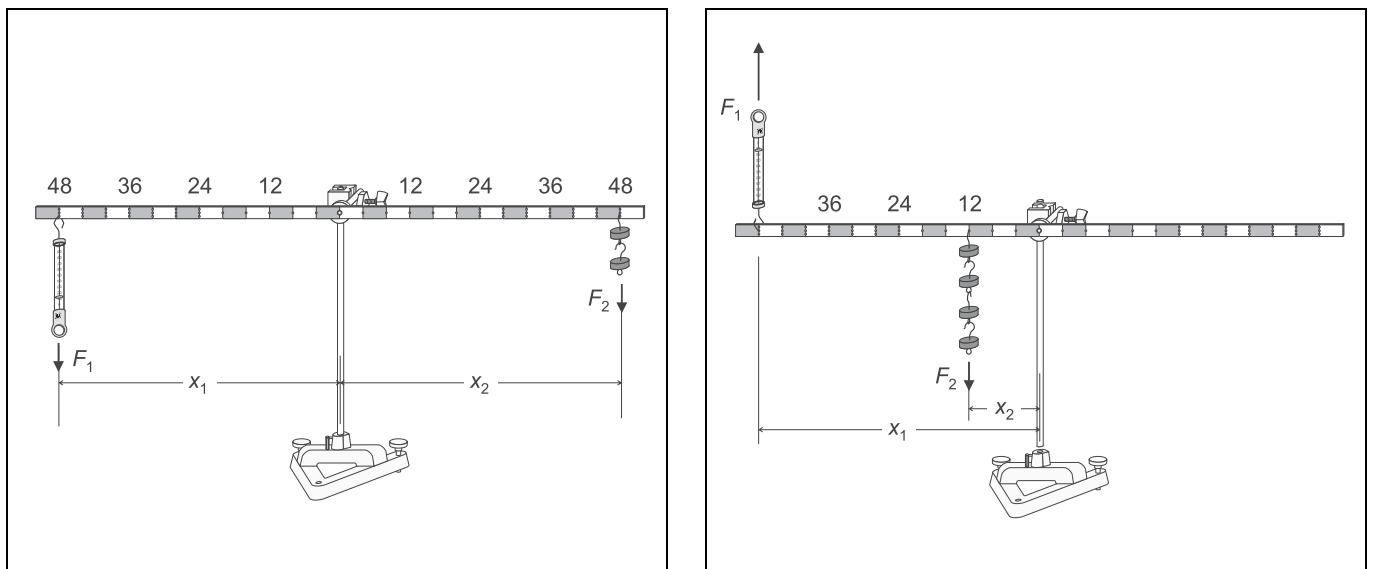
The first experiment examines the law of levers for one-sided and two-sided levers. The object is to determine the force  $F_1$  which maintains a lever in equilibrium as a function of the load  $F_2$ , the load arm  $x_2$  and the power arm  $x_1$ . The load is applied using multiple 50 g weights suspended one below the other. For the load

$$F_2 = m \cdot g$$

$g$ : gravitational acceleration

of a weight, the value 0.5 N can be assumed with sufficient accuracy.

Fig. 1 Experiment setup for verifying the law of levers for a one-sided (left) and two-sided (right) lever



**Apparatus**

1 Lever, 1 m . . . . .	342 60
1 Set of 12 weights, 50 g each . . . . .	342 61
1 Dynamometer, 2 N . . . . .	314 45
1 Dynamometer, 5 N . . . . .	314 46
1 Stand base, V-shape, 20 cm . . . . .	300 02
1 Stand rod, 47 cm . . . . .	300 42
1 Leybold multiclamp . . . . .	301 01

**Setup and carrying out the experiment**

**a) Two-sided lever**

Set up the experiment as shown in Fig. 1 (top).

a1) *Measuring as a function of the load arm  $F_2$ :*

- Suspend two, four and six weights at  $x_2 = 24$  cm and attach a dynamometer 2 N at  $x_1 = 48$  cm to determine the force  $F_1$  required to maintain the lever in a horizontal position.

a2) *Measuring as a function of the load arm  $x_2$ :*

- Suspend four weights at  $x_2 = 48, 36$  and  $24$  cm and attach a dynamometer 2 N at  $x_1 = 48$  cm to determine the force  $F_1$  required to maintain the lever in a horizontal position.

a3) *Measuring as a function of the power arm  $x_1$ :*

- Suspend four weights at  $x_2 = 48$  cm and attach a dynamometer 5 N at  $x_1 = 48, 36$  and  $24$  cm to determine the force  $F_1$  required to maintain the lever in a horizontal position.

**b) One-sided lever**

Set up the experiment as shown in Fig. 1 (bottom).

b1) *Measuring as a function of the load  $F_2$ :*

- Suspend four, eight and 12 weights at  $x_2 = 12$  cm and attach a dynamometer 2 N at  $x_1 = 48$  cm to determine the force  $F_1$  required to maintain the lever in a horizontal position.

b2) *Measuring as a function of the load arm  $x_2$ :*

- Suspend four weights at  $x_2 = 12, 24$  and  $36$  cm and attach a dynamometer 2 N at  $x_1 = 48$  cm to determine the force  $F_1$  required to maintain the lever in a horizontal position.

b3) *Measuring as a function of the power arm  $x_1$ :*

- Suspend three weights at  $x_2 = 48$  cm and attach a dynamometer 5 N at  $x_1 = 36, 24$  and  $12$  cm to determine the force  $F_1$  required to maintain the lever in a horizontal position.

**Measuring example and evaluation**

**a) Two-sided lever**

Table 1: Force  $F_1$  as a function of the load  $F_2$  ( $x_1 = 48$  cm,  $x_2 = 24$  cm)

$\frac{F_2}{\text{N}}$	$\frac{F_2 \cdot x_2}{\text{Nm}}$	$\frac{F_1}{\text{N}}$	$\frac{F_1 \cdot x_1}{\text{Nm}}$
1.0	0.24	0.5	0.24
2.0	0.48	1.0	0.48
3.0	0.72	1.5	0.72

Table 2: Force  $F_1$  as a function of load arm  $x_2$  ( $x_1 = 48$  cm,  $F_2 = 2.0$  N)

$\frac{x_2}{\text{cm}}$	$\frac{F_2 \cdot x_2}{\text{Nm}}$	$\frac{F_1}{\text{N}}$	$\frac{F_1 \cdot x_1}{\text{Nm}}$
24	0.48	1.0	0.48
36	0.72	1.5	0.72
48	0.96	2.0	0.96

Table 3: Force  $F_1$  as a function of power arm  $x_1$  ( $x_2 = 48$  cm,  $F_2 = 2.0$  N)

$\frac{x_1}{\text{cm}}$	$\frac{F_1}{\text{N}}$	$\frac{F_1 \cdot x_1}{\text{Nm}}$	$\frac{F_2 \cdot x_2}{\text{Nm}}$
24	4.0	0.96	0.96
36	2.75	0.99	0.96
48	2.0	0.96	0.96

**b) One-sided lever**

Tab. 4: Force  $F_1$  as a function of the load  $F_2$  ( $x_1 = 48$  cm,  $x_2 = 12$  cm)

$\frac{m_2}{\text{g}}$	$\frac{F_2}{\text{N}}$	$\frac{F_2 \cdot x_2}{\text{Nm}}$	$\frac{F_1}{\text{N}}$	$\frac{F_1 \cdot x_1}{\text{Nm}}$
200	2.0	0.24	0.5	0.24
400	4.0	0.48	1.0	0.48
600	6.0	0.72	1.5	0.72

Table 5: Force  $F_1$  as a function of load arm  $x_2$  ( $x_1 = 48$  cm,  $F_2 = 2.0$  N)

$\frac{x_1}{\text{cm}}$	$\frac{F_2 \cdot x_2}{\text{Nm}}$	$\frac{F_1}{\text{N}}$	$\frac{F_1 \cdot x_1}{\text{Nm}}$
12	0.24	0.5	0.24
24	0.48	1.0	0.48
36	0.72	1.5	0.72

Table 6: Force  $F_1$  as a function of power arm  $x_1$  ( $x_2 = 48$  cm,  $F_2 = 1.0$  N)

$\frac{x_1}{\text{cm}}$	$\frac{F_1}{\text{N}}$	$\frac{F_1 \cdot x_1}{\text{Nm}}$	$\frac{F_2 \cdot x_2}{\text{Nm}}$
12	4.0	0.48	0.48
24	2.0	0.48	0.48
36	1.25	0.45	0.48

**Results**

For one-sided and two-sided levers, the law of levers applies: "force x power arm = load x load arm".